

Evaluate the following integral counterclockwise. $\oint_C \cot \frac{z}{4} dz$ where C: $|z|=1$. [97 中央機械能源
光機電生醫 7]

[解]令 $f(z) = \cot \frac{z}{4} = \frac{\cos \frac{z}{4}}{\sin \frac{z}{4}}$, $f(z)$ 有單極點在 $z=0$

$$R_0 = \left. \frac{\cos \frac{z}{4}}{\frac{1}{4} \cos \frac{z}{4}} \right|_{z=0} = 4$$

$$\oint_C \cot \frac{z}{4} dz = 2\pi i \cdot R_0 = 8\pi i$$