

Find the equation of the plane containing the point $(2, -3, 4)$ and orthogonal to the vector $\mathbf{A} = 8\mathbf{i} - 6\mathbf{j} + 4\mathbf{k}$. [103雲科大電機4(2)]

[解]設 $P(2, -3, 4)$, 平面上任一點為 $X(x, y, z)$, 則

$$\mathbf{A} \cdot \overrightarrow{PX} = 0 \Rightarrow (8\mathbf{i} - 6\mathbf{j} + 4\mathbf{k}) \cdot [(x-2)\mathbf{i} + (y+3)\mathbf{j} + (z-4)\mathbf{k}] = 0$$

$$8(x-2) - 6(y+3) + 4(z-4) = 0 \Rightarrow 4x - 3y + 2z = 25$$