

Write down the definition of divergence (div). Find the div of the given vector function $\mathbf{v} = (z - y)\mathbf{i} + (x - z)\mathbf{j} + (y - x)\mathbf{k}$. [104 高應大機械乙 5(1)]

[解]若 $\mathbf{v} = v_1\mathbf{i} + v_2\mathbf{j} + v_3\mathbf{k}$, 則 $\text{div } \mathbf{v} = \nabla \cdot \mathbf{v} = \frac{\partial v_1}{\partial x} + \frac{\partial v_2}{\partial y} + \frac{\partial v_3}{\partial z}$

此題 $v_1 = z - y$, $v_2 = x - z$, $v_3 = y - x$, 因此 $\nabla \cdot \mathbf{v} = 0$