

In complex analysis find $\cos(5i + 3)$. [103 中正光電 5]

$$\begin{aligned} [\text{解}] \cos(5i + 3) &= \cos 5i \cos 3 - \sin 5i \sin 3 = \frac{e^{i(5i)} + e^{-i(5i)}}{2} \cdot \cos 3 - \frac{e^{i(5i)} - e^{-i(5i)}}{2i} \cdot \sin 3 \\ &= \frac{e^{-5} + e^5}{2} \cdot \cos 3 - \frac{e^{-5} - e^5}{2i} \cdot \sin 3 = \cosh 5 \cos 3 - i \sinh 5 \sin 3 \end{aligned}$$



Southern Taiwan University of Science and Technology